CDIO

Continuous Distribution of Interdomain Orientations

User Manual

YANG QI, TERRENCE G. OAS AND BRUCE R. DONALD

COPYRIGHT (C) 2015 BRUCE DONALD LAB, DUKE UNIVERSITY

Contents

1	Introduction	2
	1.1 Motional Decoupling and Saupe Tensors	. 2
	1.2 The Bingham Distribution on $SO(3)$. 2
	1.3 The Branch and Bound Algorithm	2
2	Setting up and Running CDIO	3

Chapter 1

Introduction

CDIO is the first fitting program to determine a continuous interdomain orientation distribution from motionally decoupled dynamic NMR data. CDIO is our first step on a sound mathematical ground to reconstruct the conformational distribution of biological macromolecules. Underlying the MATLAB code of CDIO, there are two key components, a continuous model that describes a broad spectrum of interdomain motions and a de novo Branch-and-Bound algorithm that guarantees to find the best-fit. CDIO is applicable to the study of interdomain motions in protein, RNA or DNA molecules. CDIO only requires two alignment tensors of each domain calculated either from residual dipolar couplings or pseudo-contact shifts to determine the best-fit interdomain orientation distribution. CDIO is developed jointly in the lab of Prof. Bruce Donald and the lab of Prof. Terrence Oas at Duke University.

CDIO is free software and can be redistributed and/or modified under the terms of the GNU Lesser General Public License as published by the Free Software Foundation, either version 3 of the License, or (optionally) any later version. CDIO is distributed in the hope that it will be useful, but WITHOUT ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU Lesser General Public License for more details. Full licensing details, including citation requirements, are found in the document license.pdf enclosed with this package distribution.

The primary contributors to this version of the CDIO distribution are: Yang Qi, Terrence Oas and Bruce Donald.

- 1.1 Motional Decoupling and Saupe Tensors
- 1.2 The Bingham Distribution on SO(3)
- 1.3 The Branch and Bound Algorithm

Chapter 2

Setting up and Running CDIO

CDIO requires MATLAB to run, but it does not require any MATLAB toolboxes. MATLAB R2013 or any later version should be sufficient. To install MATLAB, please follow the official instructions(http://www.mathworks.com/help/install/ug/install-mathworks-software.html).

In the CDIO distribution, the mhg function and its associated files are included. The copyright of the the mhg function belongs to Dr. Plamen Koev in San Jose State University [6]. You may want to recompile the mhg.c file before running. To compile the mhg.c file, type the following command at the MATLAB prompt:

mex mhg.c

The main function of the CDIO program is BnBmain. The inputs to the main function are two 2×5 matrices containing a total of four Saupe tensors. Given the Saupe tensor of the reference domain (Domain I) from two independent alignments, $S_{\rm I}^1$ and $S_{\rm I}^2$ and the Saupe tensors of the other domain (Domain II) from the two alignments, $S_{\rm II}^1$ and $S_{\rm II}^2$, the inputs ${\bf s1}$ and ${\bf s2}$ are formatted as:

$$\mathbf{s1} = [S_{\text{\tiny I}}^1(\mathbf{1},\mathbf{1}), \, S_{\text{\tiny I}}^1(\mathbf{2},\mathbf{2}), \, S_{\text{\tiny I}}^1(\mathbf{1},\mathbf{2}), \, S_{\text{\tiny I}}^1(\mathbf{1},\mathbf{3}), \, S_{\text{\tiny I}}^1(\mathbf{2},\mathbf{3}); \\ S_{\text{\tiny I}}^2(\mathbf{1},\mathbf{1}), \, S_{\text{\tiny I}}^2(\mathbf{2},\mathbf{2}), \, S_{\text{\tiny I}}^2(\mathbf{1},\mathbf{2}), \, S_{\text{\tiny I}}^2(\mathbf{1},\mathbf{3}), \, S_{\text{\tiny I}}^2(\mathbf{2},\mathbf{3})]; \\ \mathbf{s2} = [S_{\text{\tiny II}}^1(\mathbf{1},\mathbf{1}), \, S_{\text{\tiny II}}^1(\mathbf{2},\mathbf{2}), \, S_{\text{\tiny II}}^1(\mathbf{1},\mathbf{2}), \, S_{\text{\tiny II}}^1(\mathbf{1},\mathbf{3}), \, S_{\text{\tiny II}}^1(\mathbf{2},\mathbf{3}); \, S_{\text{\tiny II}}^2(\mathbf{1},\mathbf{1}), \, S_{\text{\tiny II}}^2(\mathbf{2},\mathbf{2}), \, S_{\text{\tiny II}}^2(\mathbf{1},\mathbf{2}), \, S_{\text{\tiny II}}^2(\mathbf{1},\mathbf{3}), \, S_{\text{\tiny II}}^2(\mathbf{2},\mathbf{3})]; \\ \mathbf{s2} = [S_{\text{\tiny II}}^1(\mathbf{1},\mathbf{1}), \, S_{\text{\tiny II}}^1(\mathbf{2},\mathbf{2}), \, S_{\text{\tiny II}}^1(\mathbf{1},\mathbf{2}), \, S_{\text{\tiny II}}^1(\mathbf{1},\mathbf{3}), \, S_{\text{\tiny II}}^1(\mathbf{2},\mathbf{3}); \, S_{\text{\tiny II}}^2(\mathbf{1},\mathbf{1}), \, S_{\text{\tiny II}}^2(\mathbf{2},\mathbf{3})]; \\ \mathbf{s3} = [S_{\text{\tiny II}}^1(\mathbf{1},\mathbf{1}), \, S_{\text{\tiny II}}^1(\mathbf{2},\mathbf{2}), \, S_{\text{\tiny II}}^1(\mathbf{1},\mathbf{2}), \, S_{\text{\tiny II}}^1(\mathbf{1},\mathbf{3}), \, S_{\text{\tiny II}}^1(\mathbf{2},\mathbf{3}); \, S_{\text{\tiny II}}^1(\mathbf{1},\mathbf{3}), \, S_{\text{\tiny II}}^2(\mathbf{1},\mathbf{3}), \,$$

To run the program, type the following command at the MATLAB prompt:

BnBmain(s1,s2)

When no input arguments or incorrect arguments are supplied, the program sets the input as the SpA-N data automatically. If you only want to reproduce the SpA-N result, drop the arguments and simply type:

BnBmain

Bibliography

- [1] Donald BR (2011) Algorithms in structural molecular biology (MIT Press Cambridge, MA), pp 27-46.
- [2] Bingham C (1974) An Antipodally Symmetric Distribution on the Sphere. *The Annals of Statistics* 2(6):1201-1225.
- [3] Kunze K and Schaeben H (2004) The bingham distribution of quaternions and its spherical radon transform in texture analysis. *Mathematical Geology* 36(8):917-943.
- [4] Mebius JE (2005) A matrix-based proof of the quaternion representation theorem for four-dimensional rotations. arXiv preprint math/0501249.
- [5] Prentice MJ (1986) Orientation statistics without parametric assumptions. *Journal of the Royal Statistical Society. Series B. Methodological* 48(2):214-222.
- [6] Koev P and Edelman A (2006) The efficient evaluation of the hypergeometric function of a matrix argument. *Mathematics of Computation* 75(254):833-846.
- [7] Losonczi JA, Andrec M, Fischer MW, and Prestegard JH (1999) Order matrix analysis of residual dipolar couplings using singular value decomposition. *Journal of Magnetic Resonance* 138(2):334-342.
- [8] Ruan K and Tolman JR (2005) Composite alignment media for the measurement of independent sets of NMR residual dipolar couplings. Journal of the American Chemical Society 127(43):15032-15033.